Geotritium: Implications of DeP Weak Interaction Fusion in Magmatic Systems

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Abstract: Tritium in the environment comes from several sources: anthropogenic nuclear weapons and commercial nuclear reactors, atmospheric cosmic-ray production, and geotritium. Geotritium and its decay product $^3$He is found in the earth’s magmatic system evidenced by tritium emission from volcanoes and $^3$He anomalies associated with MORB (Mid-Ocean Ridge Basalts), OIB (Oceanic Island Basalts) and deep mantle plumes. The $^3$He can be accounted for assuming a radiogenic $^3T(^3He)$ component as opposed to a primordial source. It is proposed that the $d(p^e^-ν)t$ weak interaction fusion (WIF) reaction ($Q = 5.474$ MeV) is the source for both the geotritium and anomalous $^3$He found in nature. The radiogenic lifetime for the WIF reaction, $\tau_{dp} = 1.61 \times 10^6$ yr, in a metal hydride geologic environment, such as FeH/FeD in the core and mantle of the earth, was calculated to be $\tau_{dp} = 1.61 \times 10^6$ yr. The anomalous $^3$He produced by the WIF reaction, a radiochronometer, was used to correlate and date mantle basalt processes deep within the earth. The $p(e^-ν)d$ WIF reaction ($Q = 1.442$ MeV) with a lifetime $\tau_{pe} = 2.54 \times 10^3$ yr. was also examined as a possible geochronometer for the formation interval of the oceans, the duration of the earth’s melting and degassing prior to the formation of the oceans. The formation age of the oceans was determined to be 3.93 billion years ago in good agreement with geologic magmatic activity and continental crust formation.

Key words: Geotritium, mantle helium, fusion, geochronology.

1. Introduction

Tritium is commonly found in the environment in the atmosphere, hydrosphere and within the earth itself, however its half-life (12.33 yr.) would seem to preclude timely geologic transport from the first two reservoirs into the mantle and ultimately back to the surface. The sources of tritium in the hydrosphere and atmosphere are mainly from anthropogenic nuclear weapons tests conducted prior to 1962, commercial nuclear reactors and cosmic-ray production in the atmosphere. In the earth, anomalous geotritium has been observed in volcanic lakes and volcanoes and correlated with $^3$He anomalies associated with MORB (Mid Ocean Ridge Basalts), OIB (Oceanic Island Basalts) and deep mantle plumes [1-3]. As in the previous study the $^3$He is accounted for assuming a radiogenic $^3T(^3He)$ component produced in a WIF (weak interaction fusion) process, $dp + e^- → ^3t + ν$ , a radioactive decay fusion process conducted in metal hydride mantle fluids and magma [1]. A radiogenic $^3T(^3He)$ component produced in the mantle of the earth can only be accounted for by assuming some form of nuclear reaction, i.e. radioactive decay [1], nuclear fission [4] or nuclear fusion [1-3, 5-6]. Although georeactors [4] are an appealing candidate given the history of the Oklo natural reactor, other fission evidence such as energy release and long-lived radioactive fission products that would accompany any radiogenic $^3T(^3He)$ to the surface is lacking. Additionally, conventional free space nuclear fusion reactions of interest here such as $p + d → ^3He + γ$ , $d + d → ^3t + n$ and $d + d → ^3He + p$ are excluded since there is no evidence or acceptable theory these reactions occur in solids under conditions existing in the earth’s mantle. However, electron capture radioactive decay such as $pp + e^- → d + ν_e$. 

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and \( dp + e^- \rightarrow ^3t + \nu_e \), termed WIF processes [1], can occur with very long lifetimes \((10^7 - 10^{12}) \text{yr}\) because: (a) the core and mantle temperature, pressure and particle densities are sufficiently high to allow a substantial geological reaction rate between the three particles in a metal hydride lattice matrix, and (b) the effect of the quantum tunneling through the coulomb barrier of the two charged protons in the presence of the electronic field (electrons) of a metal ion such as Fe largely cancels the Gamow penetrability factor allowing a low energy weak interaction nuclear reaction to occur. Notably, in the solar environment the WIF reactions, \( pp + e^- \rightarrow d + \nu_e \) and \( pp + e^- \rightarrow d + \nu_e ^+ \) are why the sun shines by providing deuterium fuel for nuclear fusion reactions in the sun.

The \( dp + e^- \rightarrow ^3t + \nu_e \) WIF reaction and subsequent tritium beta decay to \(^3\text{He}\) is important with regard to a possible radio chronometric \(^3\text{He}\) component that would allow dating basalt processes in geologic time. The question of whether radiogenic \(^3\text{He}\) has contributed appreciably to the \(^3\text{He}/^4\text{He}\) ratio anomalies observed between the atmospheric, oceanic seawater, MORB, OIB and deep mantel “hot-spot” plumes is an interesting and timely one (see Parman [7], commentary by Ladbury [8] and Anderson [9]). The standard accepted interpretation of helium isotopic anomalies reported in the literature over the past four decades has been based on a “primordial or protosolar” \(^3\text{He}\) content of the earth’s core and mantle [10-28]. The present interpretation of a radiogenic source of \(^3\text{He}\) produced from geotritium decay to be used as a geochronometer of magmatic processes is both novel and controversial yet this new paradigm can be shown to resolve longstanding major differences between MORB, OIB and plume helium anomalies derived from the premise of the primordial \(^3\text{He}\) concept [1, 7]. Additionally the new paradigm of a radiogenic \(^3\text{He}\) component could lead to better defining the geochronology of the D/H, U and Th abundances in the continental crust [29] and in the differentiated upper and lower mantle (See references 1-13 in Ref. [18]).

2. Mineral Physics, Lattice Vibrations and WIF Nuclear Reactions

The solar lifetime for the \( pp \rightarrow d + e^- + \nu_e \) and \( pp + e^- \rightarrow d + \nu_e ^+ \) WIF reactions depend mainly on the density of protons and electrons, the Gamow penetrability factor and temperature in the sun [30, 31]. It is not at all obvious that PeP or PeD processes should proceed in low temperature geologic settings. However, theoretical optical model investigations into ultra-low energy two- and three-body nuclear interactions by Kim and Zubarev [32-34] indicate that a combination of Thomas-Fermi electronic shielding [35, 36] coupled with a very weak long range attractive imaginary (elastic + fusion) scattering potential allows for the Gamow Factor Cancellation, the GFC effect. Additionally, mineral physics of lattice vibrations thermally excited above the Debye temperature provide for particle-hole excitations within the electronic conduction band [37, 38] uniquely producing highly mobile protons and deuterons which share the electronic environment of the metal lattice with the electrons. It is important to note that the \( pp \rightarrow d + e^- + \nu_e \) reaction does not require the electrons of Fe and therefore does not have a LRAI (long range attractive interaction) in the metal lattice. Without the assistance of the electronic Fermi contact potential in Fe, the screening potential for the pp and pd reactions are only 43.4 eV. This “effective energy or temperature” is insufficient to produce the necessary GFC effect.

2.1 GFC (Gamow Cancellation Factor)

The Kim-Zubarev GFC mechanism [32-34] with a LRAI and in combination with a Fermi contact potential is used in a low energy nuclear reaction theory to investigate the PeP and PeD weak interaction decay lifetimes in the earth’s early geological environment when melting, degassing and
differentiation were occurring to create the first continental crust, oceans and atmosphere. The main premise is the earth’s primordial hydrogen isotopes, chemically bound as iron hydrides in either the Fe core or the Fe-silicate mantle, decayed into deuterium or tritium (subsequently $^3$He) via WIF nuclear reactions during the time interval between the accretion of the earth 4.55 billion years ago and the degassing and formation of the early continental crust, MORB, oceans and atmosphere. The basic assumption is that proton and deuterium WIF reactions occur in the earth’s Fe core or Fe-silicate mantle at thermal energies above the Debye temperature (750 K) and the rate of production of deuterium and tritium is largely determined by (1) the Thomas-Fermi electron screening energy of the protons and deuterons in Fe, (2) the GFC effect and (3) the hydrogen isotope density. Details of the optical model formulation of ultra-low energy WIF fusion reactions can be found in Ref. [1] whereas a brief summary is provided by the following.

2.2 Debye Temperature

At temperatures above the Debye temperature ($\theta_D$) of a metal or ceramic hydride, protons and deuterons becomes mobile as hole-state’s with the electrons occupying the conduction band. The ceramic perovskites with oxygen vacancies created at elevated temperatures readily absorb water, followed by the hydroxyl groups filling the vacancies thus creating mobile protons and deuterons at temperatures above $\theta_D = 750$ K [39-44]. The high density and short 0-0 distance in MgSi Oxides favors hydration and proton migration. Thermally excited proton-electron particle-hole continuum states with hopping frequencies > 1E(+13) per sec are effectively developed by electronic screening potentials of the order of a keV in the vibrational lattice of Fe materials commonly found in geological settings, such as the earth’s Fe core or in the mantle perovskites, Mg(Fe)Si Oxides.

2.3 Screening Potential

A key element in the theory is a LRAI in the imaginary scattering potential [32-34] resulting from the formation of an internal electric field ($E_{\text{int}}$) in the metal ion lattice given by

$$E_{\text{internal}} = -\nabla U_{sc} - \frac{\partial A_c}{\partial t}$$  (1)

where $U_{sc}$ is the electronic screening potential and $A_c$ the Fermi Contact Potential for the electron-proton interaction at $r = 0$ [45, 46], the LRAI. This form of an induced internal electric field is commonly known as a displacement potential.

The screening potential $U_{sc}$ is the Thomas Fermi screening energy [35, 36] given by

$$U_{sc} = 30.7Z_aZ_b(Z_a^{2/3} + Z_b^{2/3})^{1/2} eV$$  (2)

with $Z_a = 1$ and $Z_b = 26$, yields a screening potential energy of 2.496 keV for the three body system, PeP or PeD, in the Fe or Fe-Silicate lattice. The screening potential is an “effective energy or temperature” for the PeP or PeD reactions to be used in the GFC formulation. The calculated value of 2.496 keV is greater than the equivalent central core temperature of the sun (< 1.35 keV).

2.4 The Reaction Rates

The PeP and PeD reaction rates in the earth core and mantle at “effective energies or temperatures” of 2.496 keV (29x10^6 K) are comparable to the solar core, 1.293 keV (15x10^6 K) and is given by:

$$R_{pp} \approx 1.102x10^{-4} \left( \frac{\rho}{\mu_e} \right) T_6^{-1/2} (1 + 0.02T_6) R_{pp}$$  (3)

or reduced to,

$$R_{pp} = \chi_{pp} R_{pp}$$  (4)

where $\mu_e$ is the mean molecular weight per electron, $\rho$ the local proton or deuteron density and $\chi_{pp}$ is understood to represent the quantities in front of $R_{pp}$ in Eq. (3).

The proton-proton or proton-deuteron rate ($R_{pp}$) is
given by:
\[
R_{pp, pd} = \frac{n_a n_b}{1 + \delta_{ab}} \langle \sigma v \rangle \tag{5}
\]
where \(n_{a,b}\) are the particle densities, \(1 + \delta_{ab}\) is the Kronecker delta which prevents double counting and the average cross section times velocity is approximated by \(\langle \sigma v \rangle\).

The comparison of the rates in the earth and sun reduces to the following equation:
\[
R_{\text{earth}}^{\text{pp}} = \frac{1}{1.01 \times 10^{10} \text{ yr}} \left( \chi_{\text{earth}} / \chi_{\text{sun}} \right)
\]
\[
\left( \frac{n_{ab}}{n_{ab}} \right) \left( \frac{E_{\text{sun}}}{U_{\text{sc}}} \right) e^{2 \pi \eta / E_{\text{sun}}} \left( \frac{\nu_e}{\nu_e} \right) \tag{6}
\]

The energies are converted to \(T_6\) temperatures \(U_{sc} = k_B T_6\), the mean molecular weight per electron (earth) = 2, average mantle density \(\rho_{\text{mantle}} = 3.84 \text{ g cm}^{-3}\) and mantle proton particle density \(n_{ab} = (1.44 - 1.65) \times 10^{22}\), equivalent to one conduction electron or particle-hole state per perovskite molecule, a 0.6% proton fraction, whereas for deuterons in the PeD reaction one uses \(D/H = 1.5 \times 10^{-4}\). The solar parameters were taken from Bahcall [30] (see his tables 4.4 and 4.5). The uncertainty is approximately \(\pm 15\%\) based on a 10% uncertainty in the overall PeP solar rate [30] and the range of mantle densities [37].

The calculated lifetimes are: (1) PeP WIF lifetime in the mantle of \(\tau_{\text{pp}} = (2.45 \pm 0.38) \times 10^{12} \text{ yr}\) which is comparable to the lifetime in the sun of \(\tau_{\text{pp}} = 4.34 \times 10^{12} \text{ yr}\), and (2) PeD WIF lifetime in the mantle of \(\tau_{\text{pd}} = (1.61 \pm 0.18) \times 10^9 \text{ yr}\). The PeD reaction lifetime is much shorter than the PeP lifetime due to the greater beta decay energy (5.474 MeV versus 1.442 MeV). The nuclear beta decay matrix elements are constant, the lifetime follows the well-known power law \(\tau^{-1} \propto E_{\beta}^{5.8}\). The PeD reaction in the earth is expected to be in secular equilibrium with the PeP reaction.

3. Isotope Anomalies in the Mantle and Ocean

During the evolution and development of a differentiated core, mantle and crust the molten earth degassed magmatic fluids that escaped to the surface of the earth to form the oceans and primitive atmosphere. The combined processes of core-mantle differentiation, degassing, ocean formation and heat loss cooled the earth allowing the mantle to evolve into cratons and primitive continental plates. The earth has a distinctive mode of planetary differentiation. Radioisotope dating of zircons using Sr, Nd, Hf and Pb have established that early Archean mantle gneisses formed at about 3.9 Gyr followed by episodic mantle activity up to the present [7, 47-49]. The same is true for the evolution of the continental crust which covers about a third of the earth’s surface today [49]. Studies of \(D/H\) and \(^3\text{He} / ^4\text{He}\) isotopic ratios therefore provide a new chronometric tool set to study magmatic processes deep within the earth over geologic time.

3.1 The \(\text{PeP} \rightarrow D + \nu_e\) WIF Reaction and Formation Age of the Oceans

The formation interval (\(\Xi\)) between the accretion of the earth 4.556 Gyr ago and the degassing and formation of the early oceans and atmosphere was calculated assuming the deuterium difference between seawater, \(D/H = (1.5 \pm 0.1) \times 10^{-4}\), and the best estimate for proto solar gas, \(D/H = (2.5 \pm 0.5) \times 10^{-5}\), or the measured Jovian atmospheric isotope ratio [50], \(D/H = (2.6 \pm 0.7) \times 10^{-5}\), resulted from the PeP WIF reaction in the earth’s early history. The formation interval equation is given as:
\[
\delta D / 2H = (1 - e^{-\lambda_{\text{pp}} t}) \tag{7}
\]
where \(\lambda_{\text{pp}} = \tau_{\text{pp}}^{-1}\), \(\tau_{\text{pp}} = (2.54 \pm 0.38) \times 10^{12} \text{ yr}\) and \(\delta D / 2H = (2.48 \pm 0.32) \times 10^{-4}\) using the Jovian measurement value [51] yields, \(\Xi = (630 \pm 160) \times 10^6 \text{ yr}\), where half of the
estimated uncertainty is from the measured uncertainties in the D/H ratios and the remainder from the pep lifetime calculation [30]. The formation age of oceans can be estimated using the accretion age of the solar system of \( (4.556 \pm 0.002) \times 10^7 \) yr [52] and the formation interval of \( \Xi = (630 \pm 160) \times 10^6 \) yr yielding \( (3.93 \pm 0.16) \times 10^6 \) yr before the present. This formation age agrees well with the appearance of the first ancient continental crust or cratons and other geologic evidence such as the water-lain sediments dated approximately to 3.8 Gyr ago [53].

3.2 The \( \text{DeP} \rightarrow \text{He} + v_e \) WIF Reaction and Helium Anomalies

Tritium concentrations in excess of atmospheric and seawater values have been observed in magmatic fluids and emanations from volcanic lakes and hot spot volcanoes such as the Kilauea (Hawaii) and Alcedo (Galapagos) [1, 2, 5]. The explosive massive eruption of Mt Ulu (Kilauea) on Hawaii in 1972 measured at an air monitoring station 100 miles away on Maui was found to have released more than 5000-Ci of tritium or a concentration of about 90 tritium atoms per liter of air [54]. The anomalous amount of tritium could not be accounted for from sources of tritium in seawater or meteoritic ground water. Likewise, tritium in the lowest layers of volcanic lakes in Europe and Turkey have been shown to store excess anomalous tritium concentrations derived from mantle fluids and volatiles [2]. The presence of excess tritium in these varied magmatic systems provides strong evidence of WIF reactions taking place in the mantle [1].

Comparing \( ^3\text{He} / ^4\text{He} \) ratios for average MORB \( (R/R_a = 8 \pm 1) \) with the range of values of OIB \( (R/R_a = 15 - 40) \) one could infer that the upper mantle has been degassed and MORB represents a depleted upper mantle with a depth of less than 670 km. Here \( (R_a = 1.39 \times 10^6) \) is the atmospheric He ratio. On the other hand, the increased He ratio for OIB and deep mantle plumes seem to indicate source’s from the lower mantle with a much longer residence time.

The lower mantle may be isolated from the upper portions over periods of several billion years [51, 55-57]. If that is the case, then WIF reactions considered here could provide a new radiogenic point of view. Assuming the difference in helium ratios of the plumes and MORB is not due to U, Th and D/H concentration changes but rather that MORB is degassed whereas the deep mantle is not, then one can calculate the increased concentration of radiogenic \( ^3\text{He} \) over the past 4.55 Gyr in the deep mantle. The maximum OIB/plume to MORB ratio is calculated to be \( R_{\text{OIB}} / R_{\text{MORB}} = (6.5 \pm 1.6) \) using the WIF lifetimes. Correcting for the decay of U and Th over the last 4.55 Gyr yields an OIB/plume ratio \( R_{\text{OIB}} = (53 \pm 13) \), a value in good agreement with what is observed experimentally.

In Fig. 1 is displayed a large compilation of experimental He ratios for MORB and OIB obtained from the literature by Parman [7].

The green and orange fields are zircon age distributions of the corresponding MORB and OIB helium ratios \( (R^{-1}) \). In the model presented above the isolated deep mantle contributes to OIB and plumes

![Fig. 1 Chronological development of MORB and OIB. The green and orange fields are zircon age distributions of the corresponding MORB (red) and OIB (green). This figure was adapted from Parman [7].](image-url)
with the upper mantle contributing to MORB. In the chronological plot the experimental red line has a lifetime of \( \tau = (1.63 \pm 0.07) \text{Gyr} \) which compares well with the calculated PeD WIF lifetime \( \tau_{\text{PeD}} = (1.61 \pm 0.18) \text{Gyr} \). Note that the estimated amount of geotritium residing in secular equilibrium in the mantle is about 1 trillion Ci or about 100 metric ton.

Some important conclusions of the Parman study [7] include: (a) the helium isotopes in OIB appear to preserve the mantle’s depletion history, (b) the helium evolution does not require a primitive or primordial mantle reservoir, (c) a correspondence between ages of mantle depletion events and crustal formation are provided by helium ratios in OIB, and (d) the helium ratios are directly proportional to the time at which sources were formed so they can be directly compared to crustal age growth. These conclusions support the present study assigning tritium and subsequent helium production in the earth’s mantle to radiogenic processes accounted for in PeD WIF reactions.

4. Conclusion

Evidence that the WIF process is responsible for helium anomalies in magmatic systems is provided by the good agreement of the calculated lifetime for the PeD WIF reaction with the lifetime of the chronological plot in Fig. 1. This new paradigm of a radiogenic \(^{3}\text{He}\) component provides a new radioactive geochronometer to date mantle processes over the lifetime of the earth.

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